

Some Recent Algorithmic Questions in Deep Reinforcement Learning

CS 285

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What Will We Discuss Today?

So far, we have gone over several interesting RL algorithms, and some theoretical aspects in RL

- Which algorithmic decisions in theory actually translate to practice, especially for Q-learning algorithms?
- Phenomena that happen in deep RL, and how we can try understanding them....
- What affects performance of various deep RL algorithms?
- Some open questions in algorithm design in **deep** RL

Disclaimer: Most material covered in this lecture is very recent and being still actively researched upon. I will present some of my perspectives on these questions in this lecture, but this is certainly not exhaustive.

Part 1: Q-Learning Algorithms

Sutton's Deadly Triad in Q-learning

Boostrapping

Off-policy Sampling

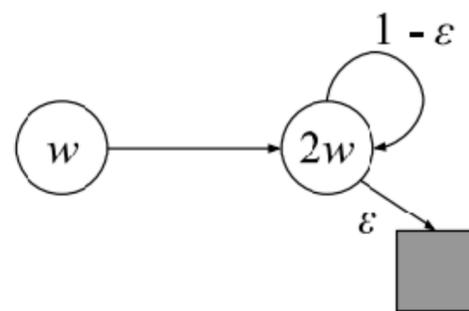
Function Approximation

$$\min_Q \mathbb{E}_{s,a \in \mathcal{D}} [((r(s, a) + \gamma Q(s', a')) - Q(s, a))^2]$$

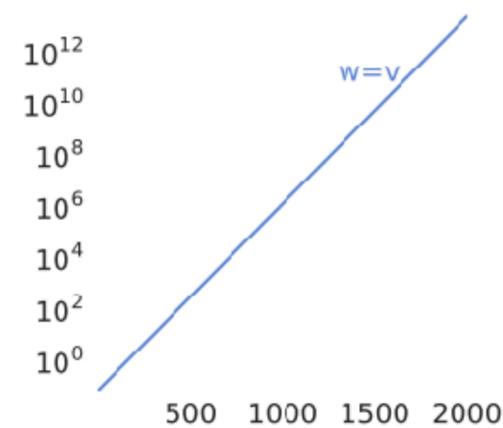
Divergence

Few parameters diverges

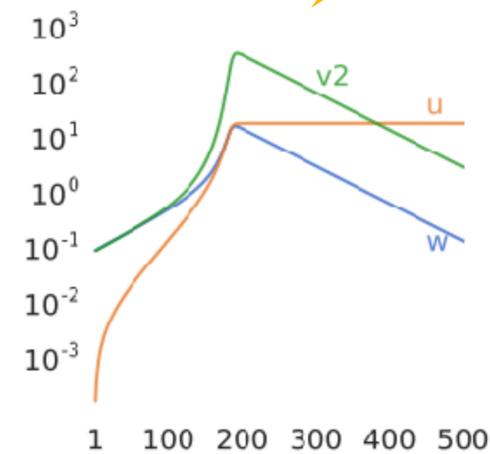
More parameters converges



(a) The example by Tsitsiklis and Van Roy (1997).



(b) $v(s) = w\phi(s)$ diverges.



(c) $v(s) = w\phi(s) + u$ converges.

More expressive functions approximators work fine?

What aspects will we cover?

- **Divergence:** Divergence can happen with the deadly triad and several algorithms tailored towards preventing this divergence. But does it actually happen in practice?

Large part of theory focused on fixing divergence

- **“Overfitting”/Sampling Error:** As with any learning problem, we would expect training neural network Q-learning schemes to suffer from some kind of overfitting. Do these methods suffer from any overfitting?

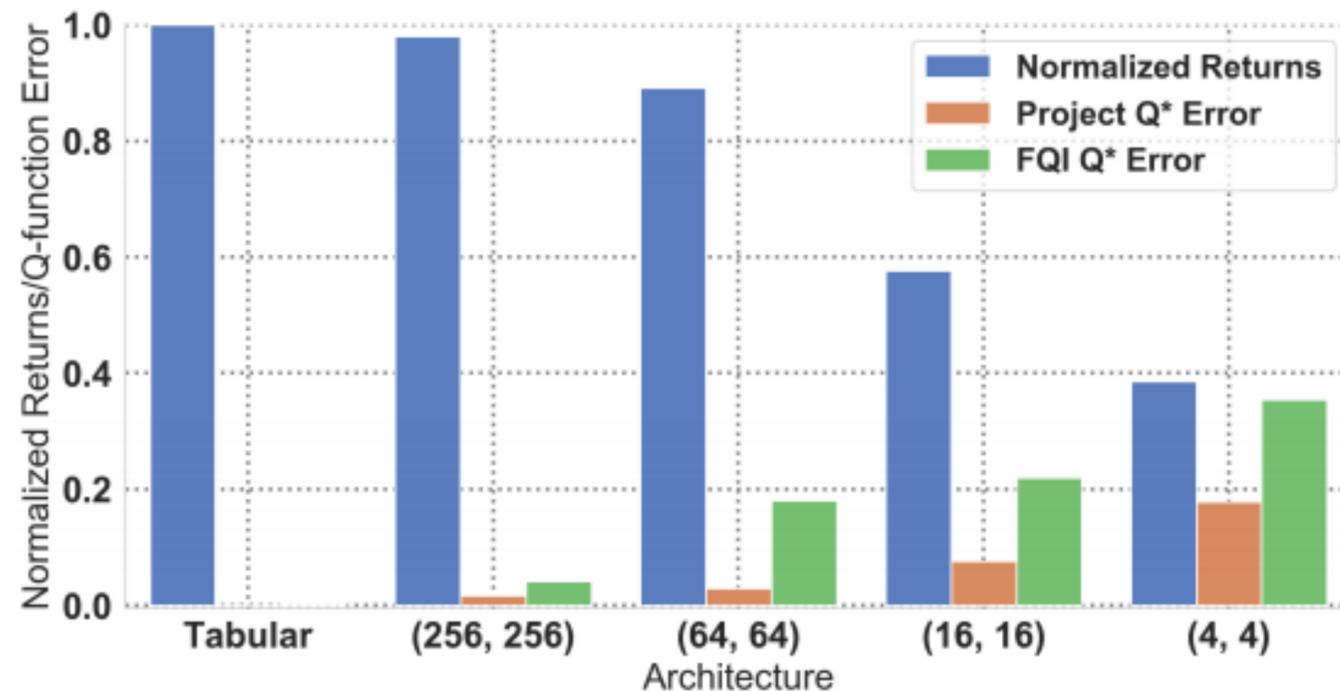
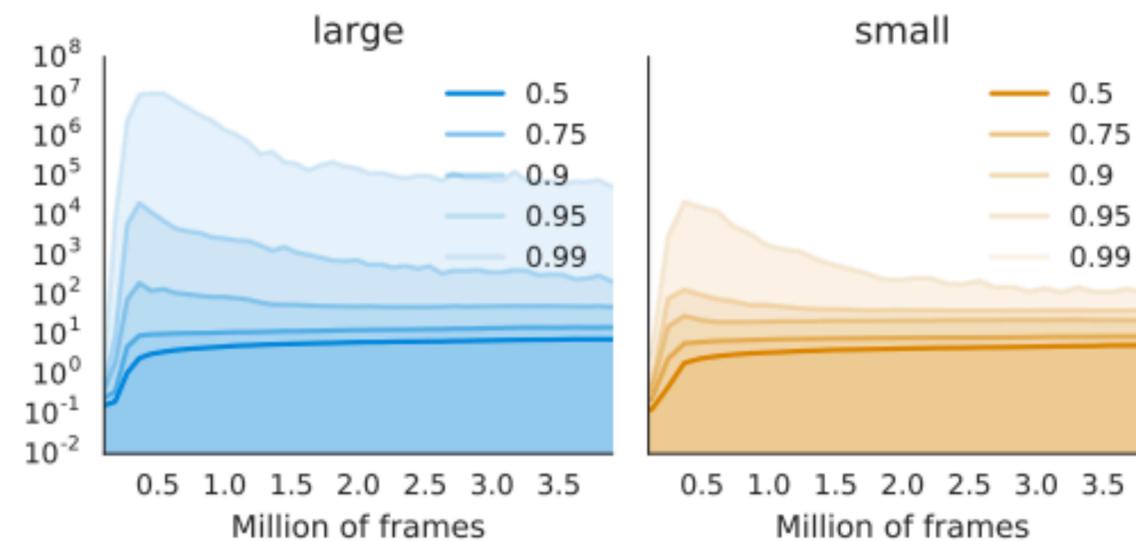
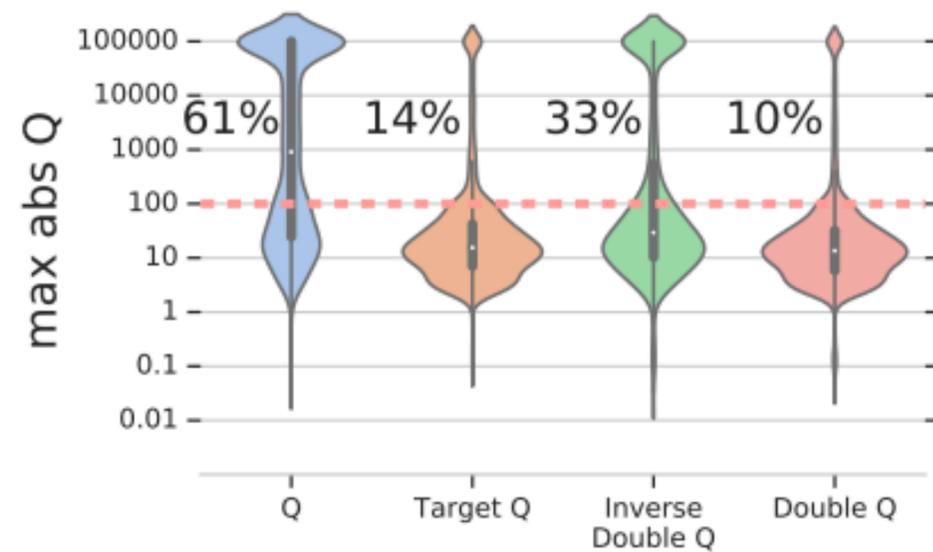
Worst-case bounds exist, but we do not know how things behave in practice

- **Data distribution:** Off-policy distributions can be bad, moreover narrow data distributions can give brittle solutions? So, which data distributions are good, and how do we get those distributions?

(Too) worst-case bounds, but how do things behave in practice?

Divergence in Deep Q-Learning

While Q-values are overestimated, there is not really significant divergence



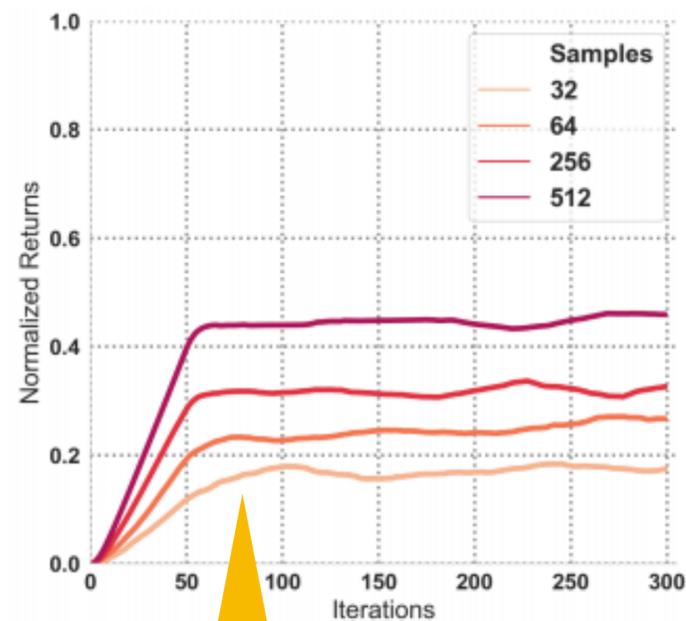
Large neural networks just seem fine in an FQI-style setting

0.9% divergence

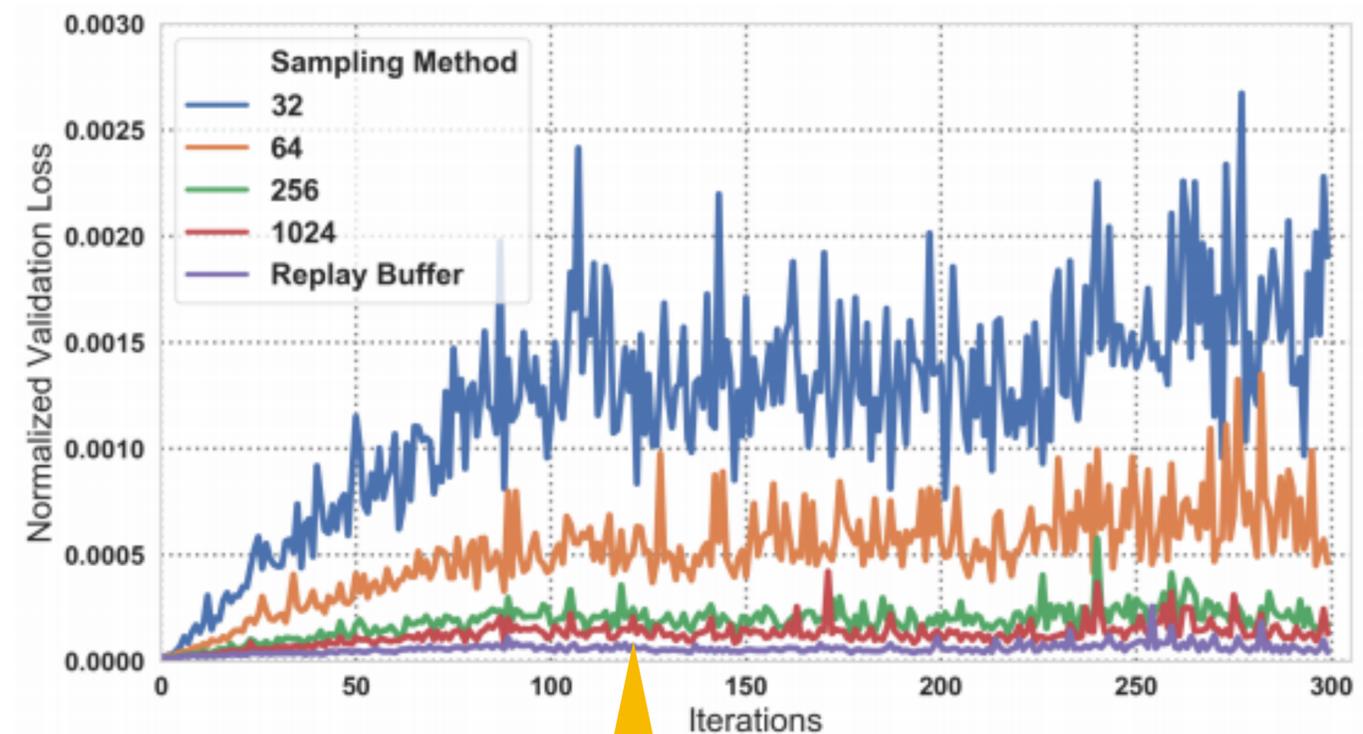
Overfitting in Deep Q-Learning

Does overfitting happen for real in FQI with neural networks?

$$\min_Q \mathbb{E}_{s, a \sim \mu} [((r(s, a) + \gamma Q(s', a')) - Q(s, a))^2] \sum_{s, a \in \mathcal{D}}$$



Few samples leads to poor performance



Replay buffer prevents overfitting, even though it is off-policy

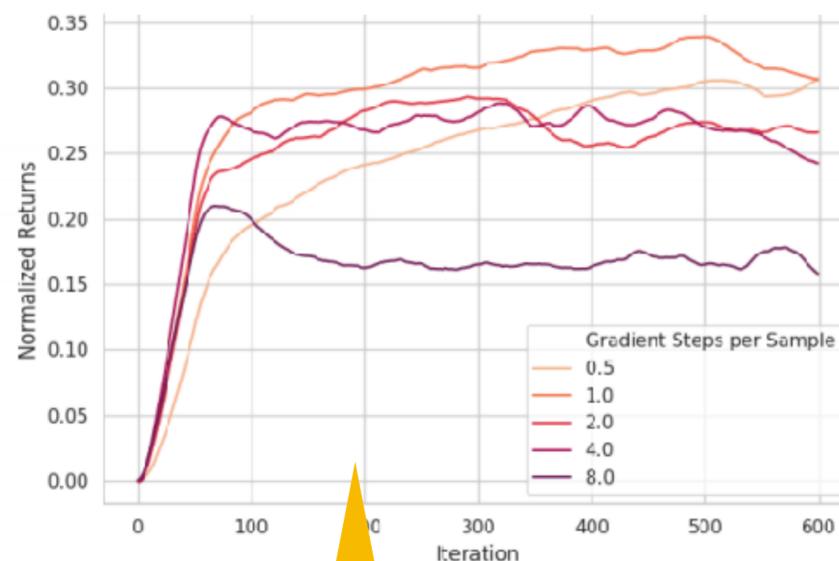
When moving from FQI to DQN/Actor-critic what happens?

Overfitting in Deep Q-Learning

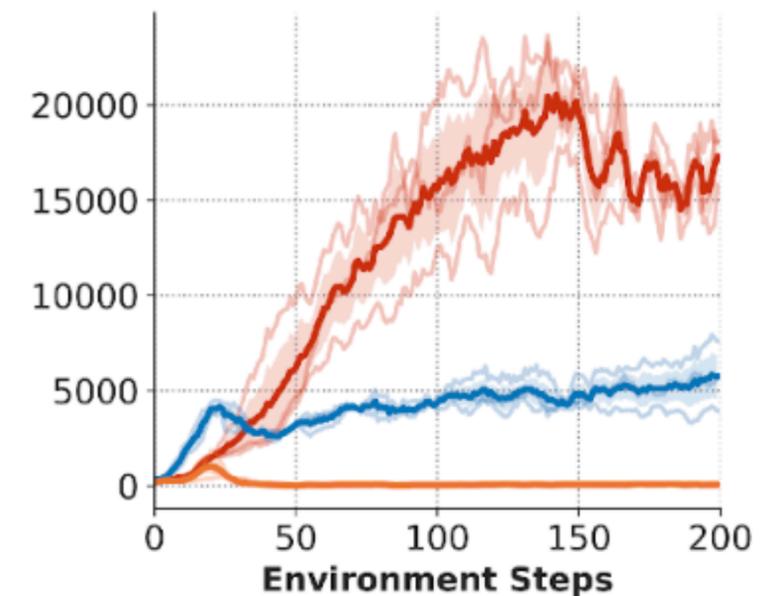
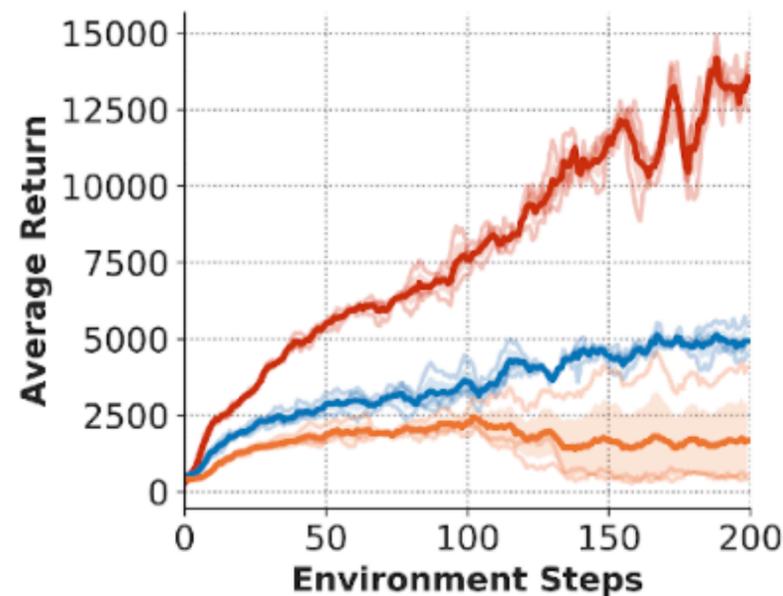
More gradient steps per environment step?

$\frac{K}{N}$ = gradient steps per environment step

1. Sample N samples from the environment
2. Train for K steps before sampling next



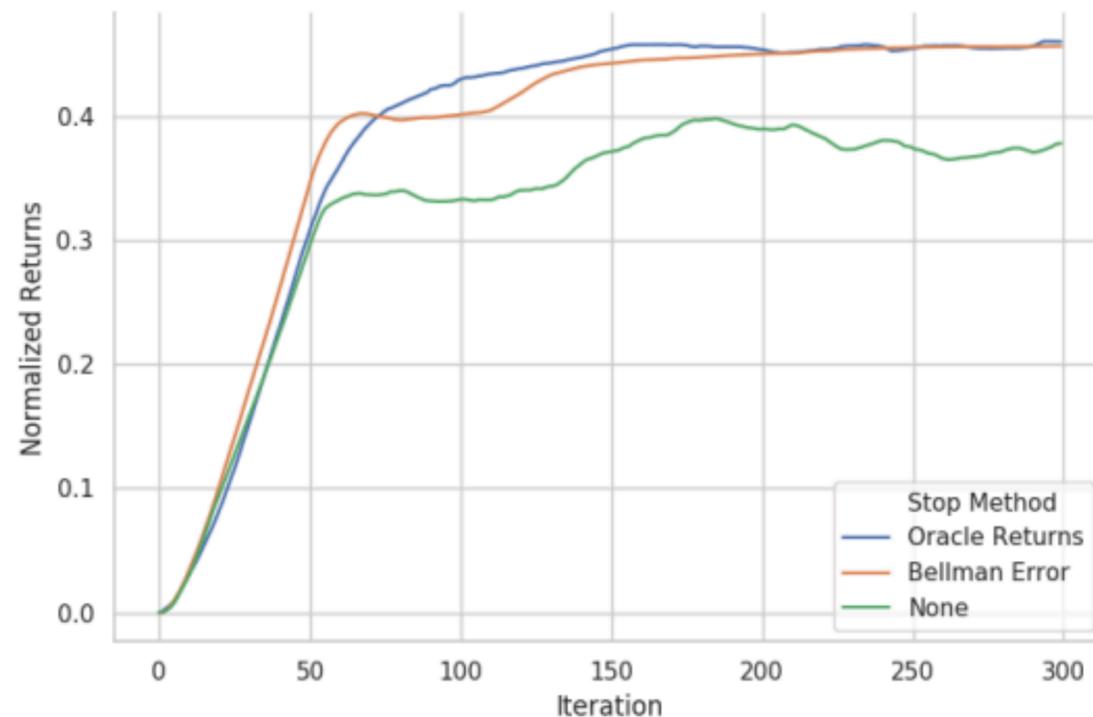
More gradient steps hurt performance



Overfitting in Deep Q-Learning

Why does performance degrade with more training?

- **Possibility 1:** Large deep networks overfit, and that can cause poor performance — so more training leads to worse performance...
- **Possibility 2:** Is there something else with the deep Q-learning update?



Early stopping helps

Although this is with “oracle access” to Bellman error on all states.... so not practical

Overfitting in Deep Q-Learning

- **Possibility 2 is also a major contributor:** Performance often depends on the fact that optimization uses a bootstrapped objective — i.e. uses labels from itself for training

Self-creating labels for training can hurt

Preliminaries: Gradient descent with deep networks has an implicit regularisation effect in supervised learning, i.e. it regularizes the solution in overparameterized settings.

$$\min_X \|AX - y\|_2^2$$

$$\min_X \|X\|_F^2 \text{ s.t. } AX = y$$

If gradient descent converges to a good solution, it converges to a minimum norm solution

Check Arora et al. (2019) for a discussion of how this regularization is more complex...

Implicit Under-Parameterization

When training Q-functions with bootstrapping on the same dataset, more gradient steps lead to a loss of expressivity due to excessive regularization, that manifests as a loss of rank of the feature matrix.

$$Q(\mathbf{s}, \mathbf{a}) = \mathbf{w}^T \Phi(\mathbf{s}, \mathbf{a}) \quad \Phi \in \mathbb{R}^{|\mathcal{S}| \times |\mathcal{A}| \times d}, \quad \mathbf{w} \in \mathbb{R}^d$$

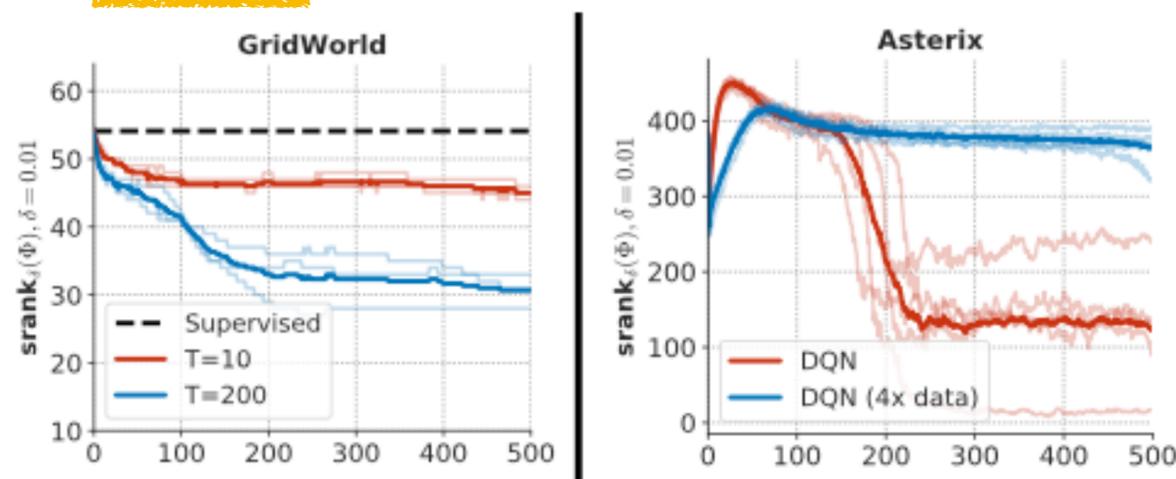
Learned by a neural network

$$\Phi = U \text{diag}\{\sigma_i(\Phi)\} V^T$$

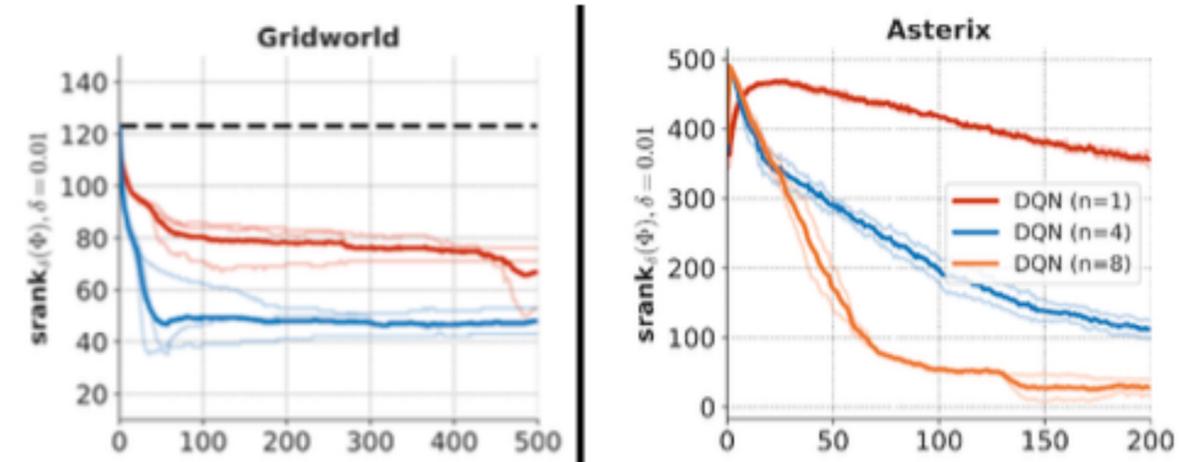
$$\text{srnk}_\delta(\Phi) = \min \left\{ k : \frac{\sum_{i=1}^k \sigma_i(\Phi)}{\sum_{i=1}^d \sigma_i(\Phi)} \geq 1 - \delta \right\}$$

Effective rank

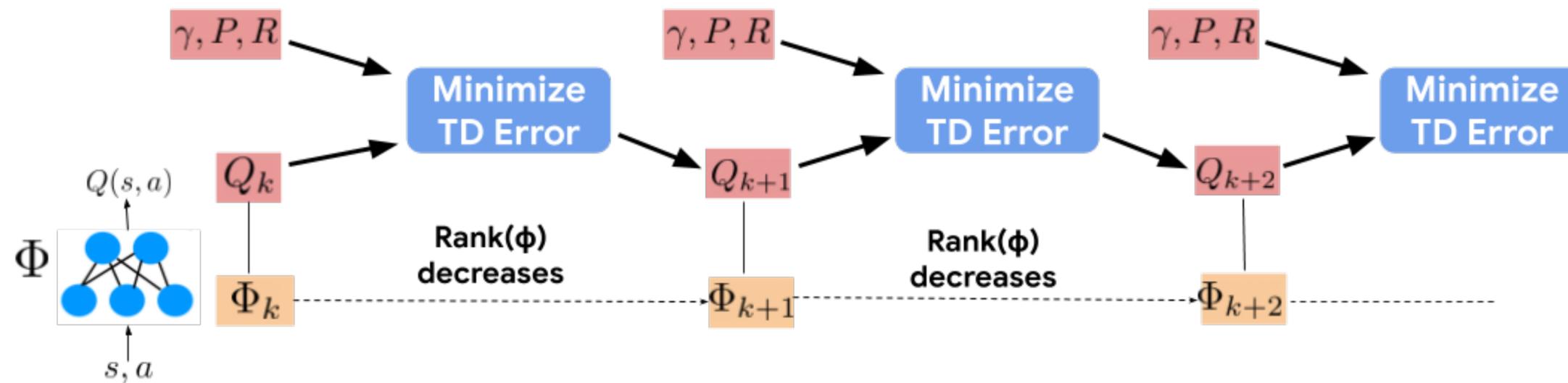
Offline



Online



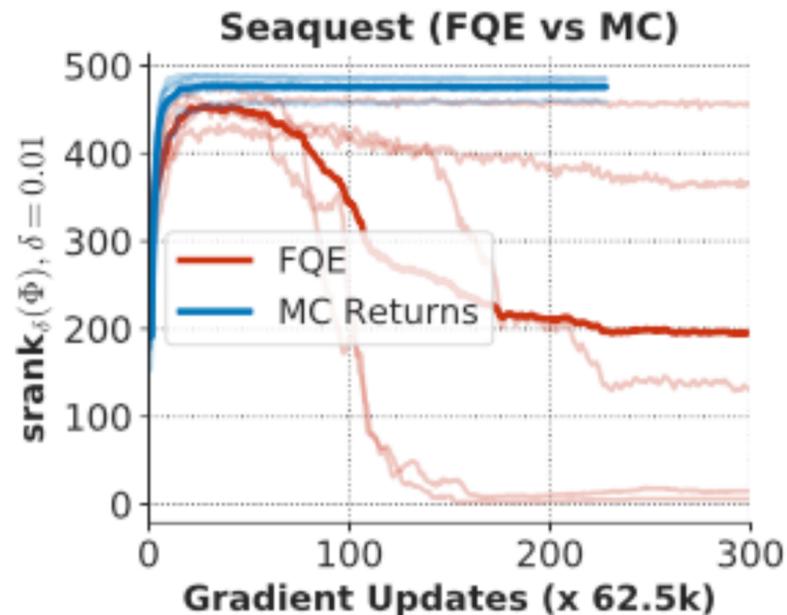
Implicit Under-Parameterization



Compounding effect of rank drop over time, since we regress to labels generated from our own previous instances (bootstrapping)

Implicit Under-Parameterization

Does implicit under-parameterization happen due to bootstrapping?



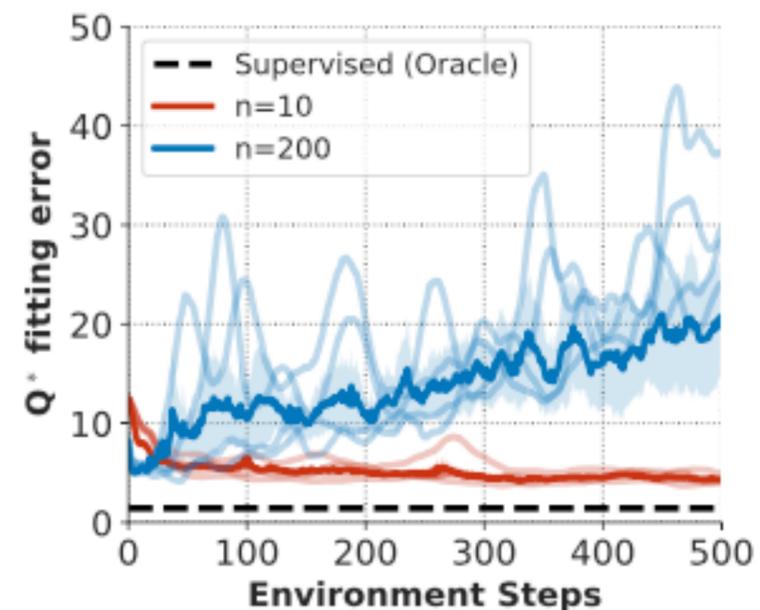
Doesn't happen when bootstrapping is absent

$$Q(s, a) = r(s, a) + \gamma E_{s', a' \sim P(s' | s, a) \pi(a' | s')} [Q(s', a')]$$

$$Q(s_0, a_0) = \sum_{t=0}^{\infty} \gamma^t r_t(s_t, a_t)$$

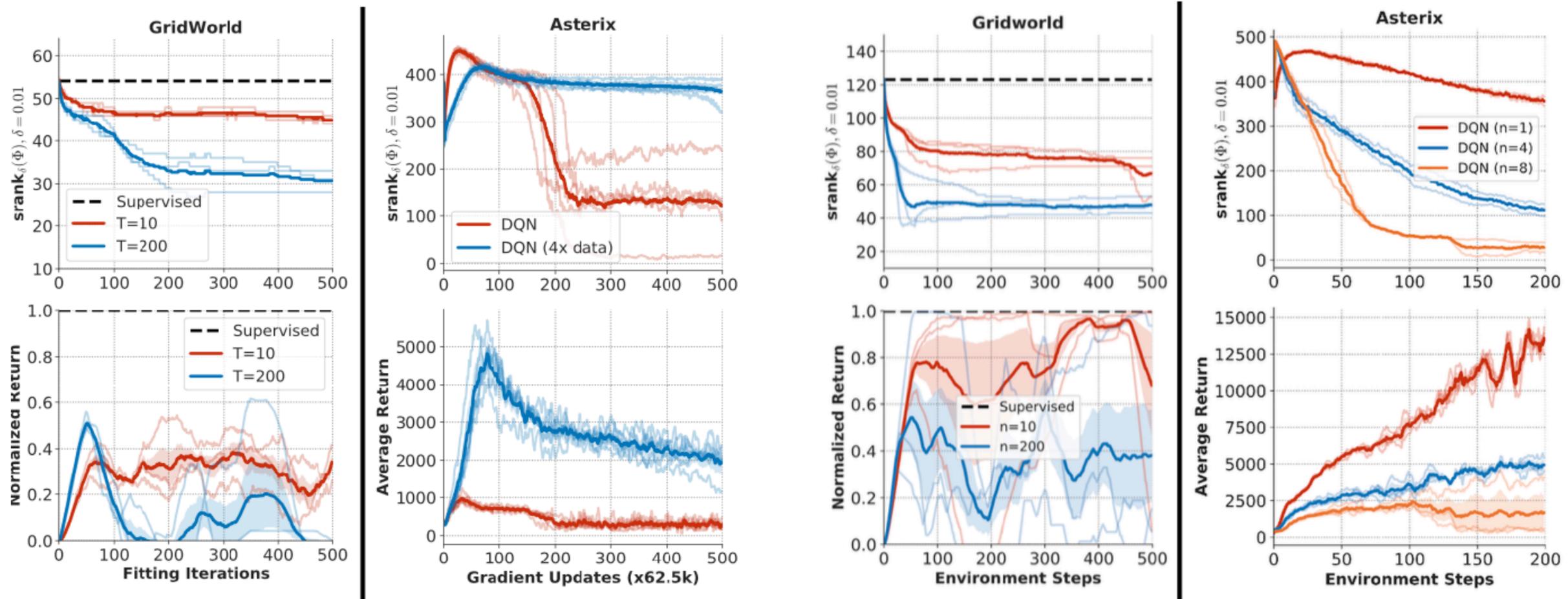
It hurts the representability of the optimal Q-function

On the gridworld example from before, representing the optimal Q-function becomes hard with more rank drop!



Effective Rank and Performance

Rank collapse corresponds to poor performance



Also observed on the gym environments, rank collapse corresponds...

Data Distributions in Q-Learning

- Deadly triad suggests poor performance due to off-policy distributions, bootstrapping and function approximation.
- Are on-policy distributions much better for Q-learning algorithms?
- If not, then what factor decides which distributions are “good” for deep Q-learning algorithms?

Experimental Setup

$$\min_Q \mathbb{E}_{s,a \sim p} \left[(Q(s, a) - (r(s, a) + \gamma \max_{a'} \bar{Q}(s', a')))^2 \right]$$

$$\mathcal{H}(p) = - \sum_{(s,a)} p(s, a) \log p(s, a)$$

Measures the entropy/
uniformity of weights

Which Data-Distributions are Good?

Compare different data distributions:

Replay

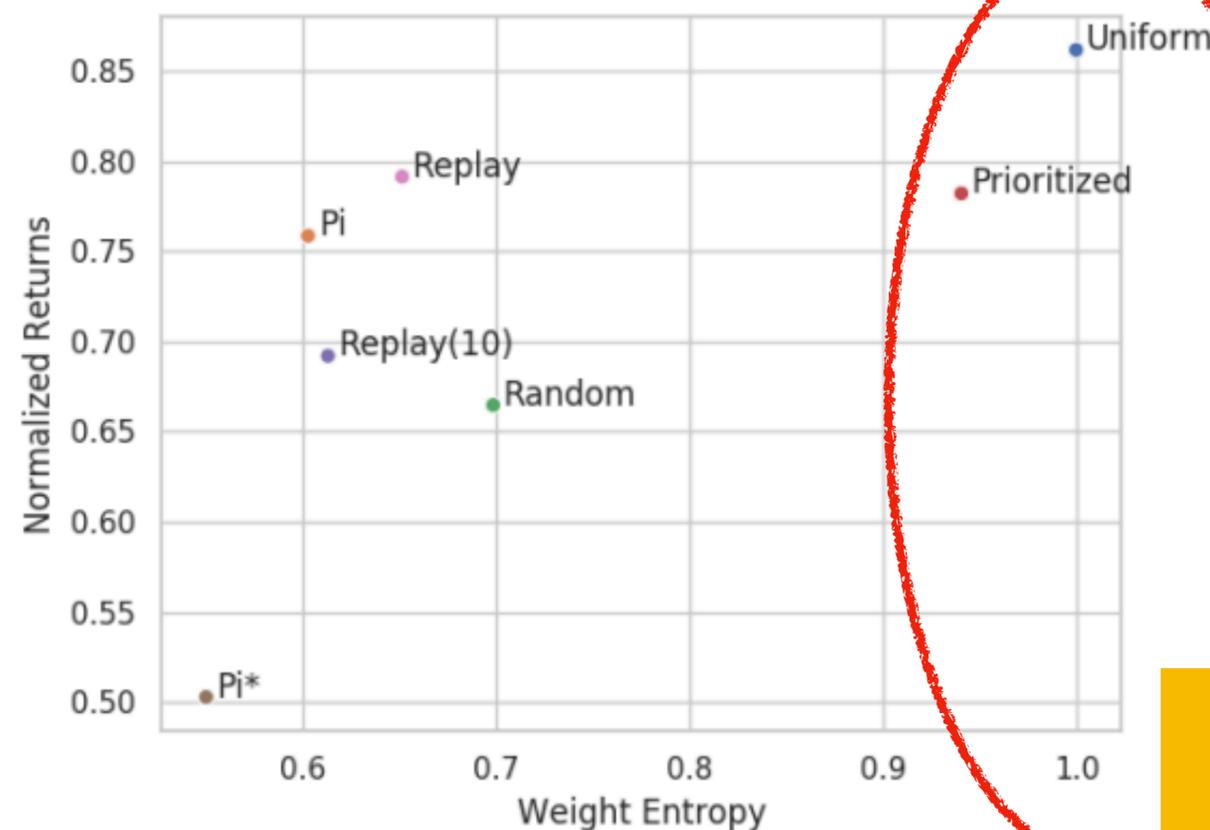
On-policy (Pi)

Optimal Policy

Uniform over (s, a)

$$\min_Q \max_p \mathbb{E}_{s,a \sim p} [(Q(s,a) - T\bar{Q}(s,a))^2]$$

Prioritized



High entropy weights are good for performance

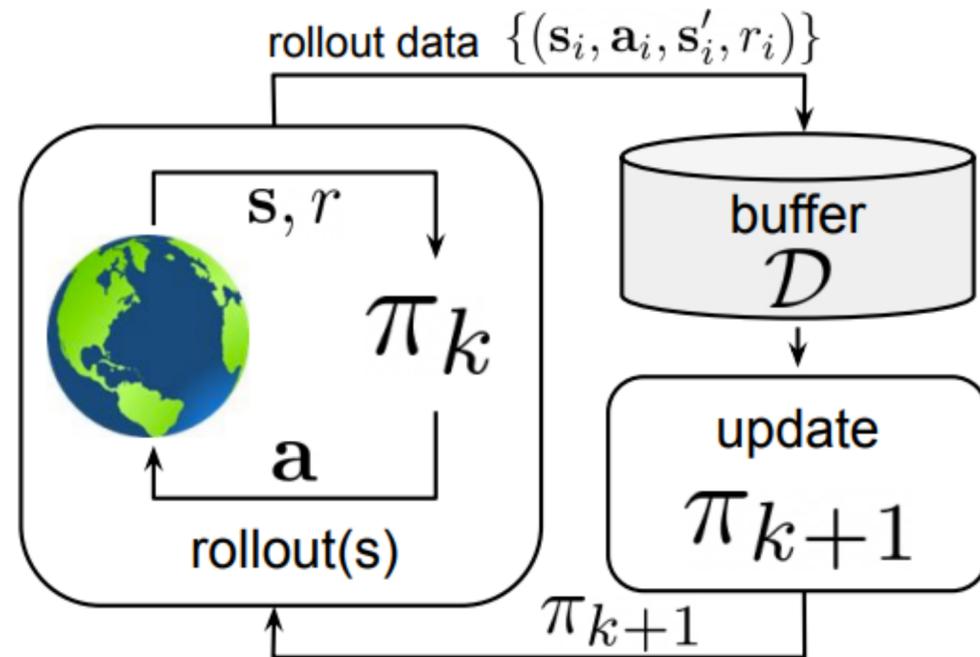
No sampling error here, all state-action pairs provided to the algorithm

Do replay buffers work because of more coverage? Maybe...

Not always, lead to biased training

$\mathcal{H}(p)$

Finding Good Data-Distributions



On-policy data collection

“Corrective Feedback” 

Corrective feedback = the ability of data collection to correct errors in the Q-function.

$$|Q_k(s, a) - Q^*(s, a)|$$

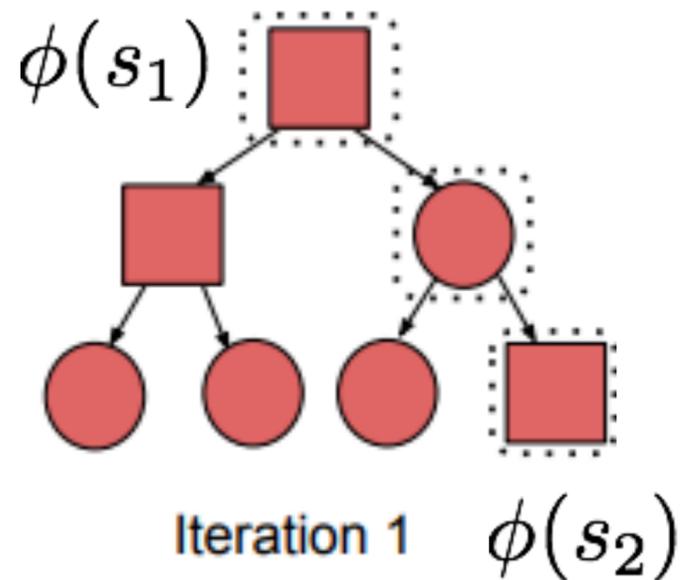
Function Approximation

Includes replay buffer distributions

What we'll show is that on-policy data collection may fail to correct errors in the target values that are important to be backed up..

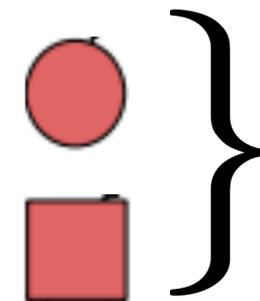
Consider This Example...

- Let's start with a simple case of an MDP with function approximation

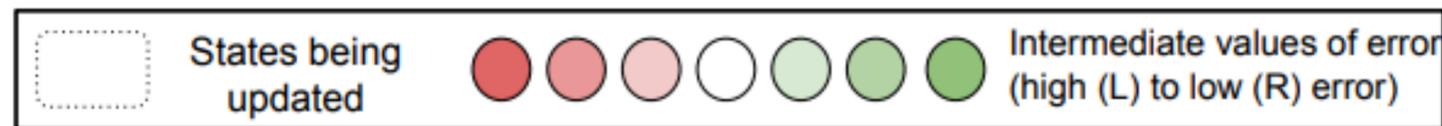


$\phi(s_1)$ and $\phi(s_2)$ are related .

$$Q(s, a) = w_a^T \phi(s)$$



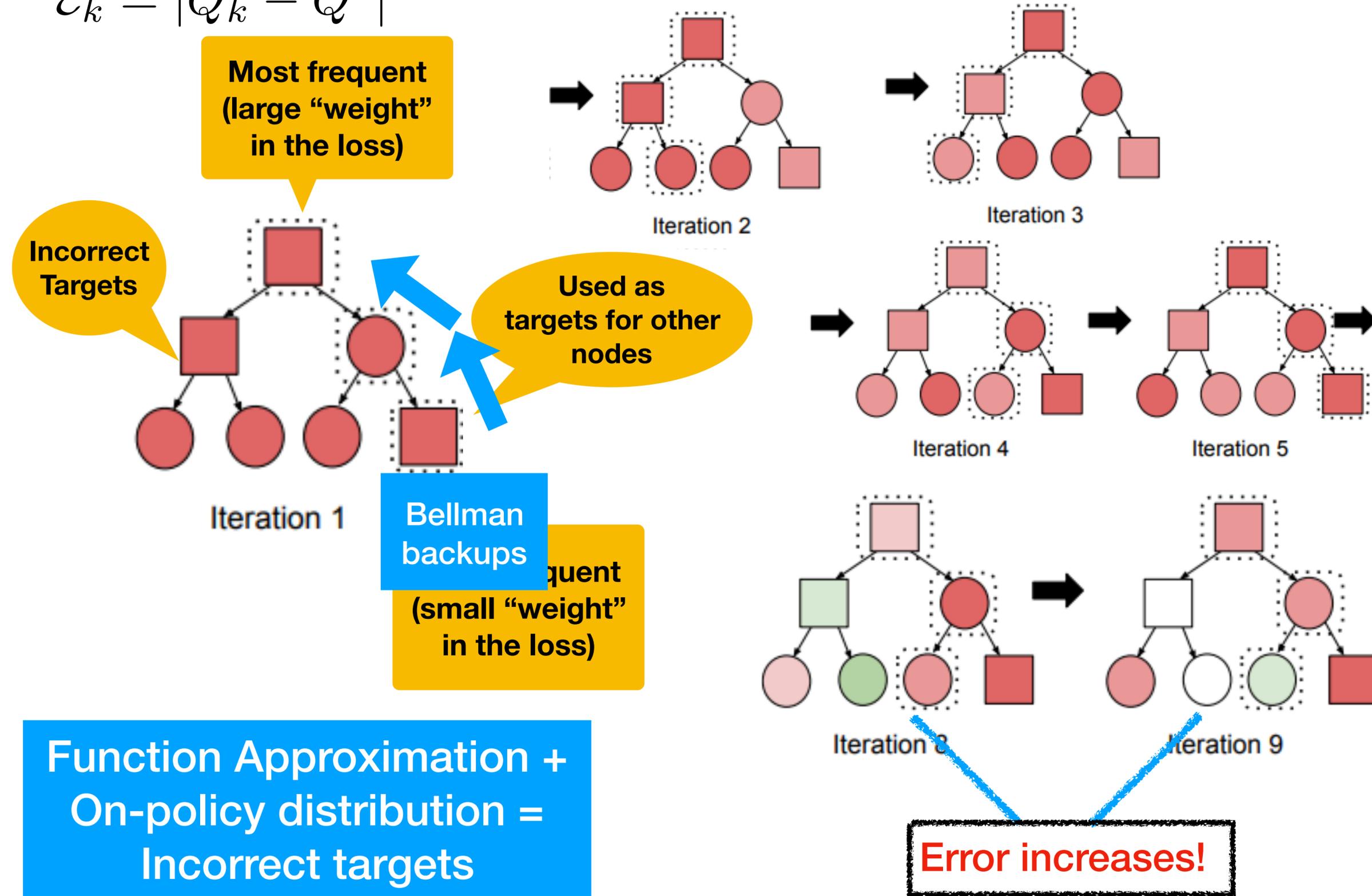
Nodes are aliased with other nodes of the same shape



Data distribution would affect solutions in the presence of aliasing

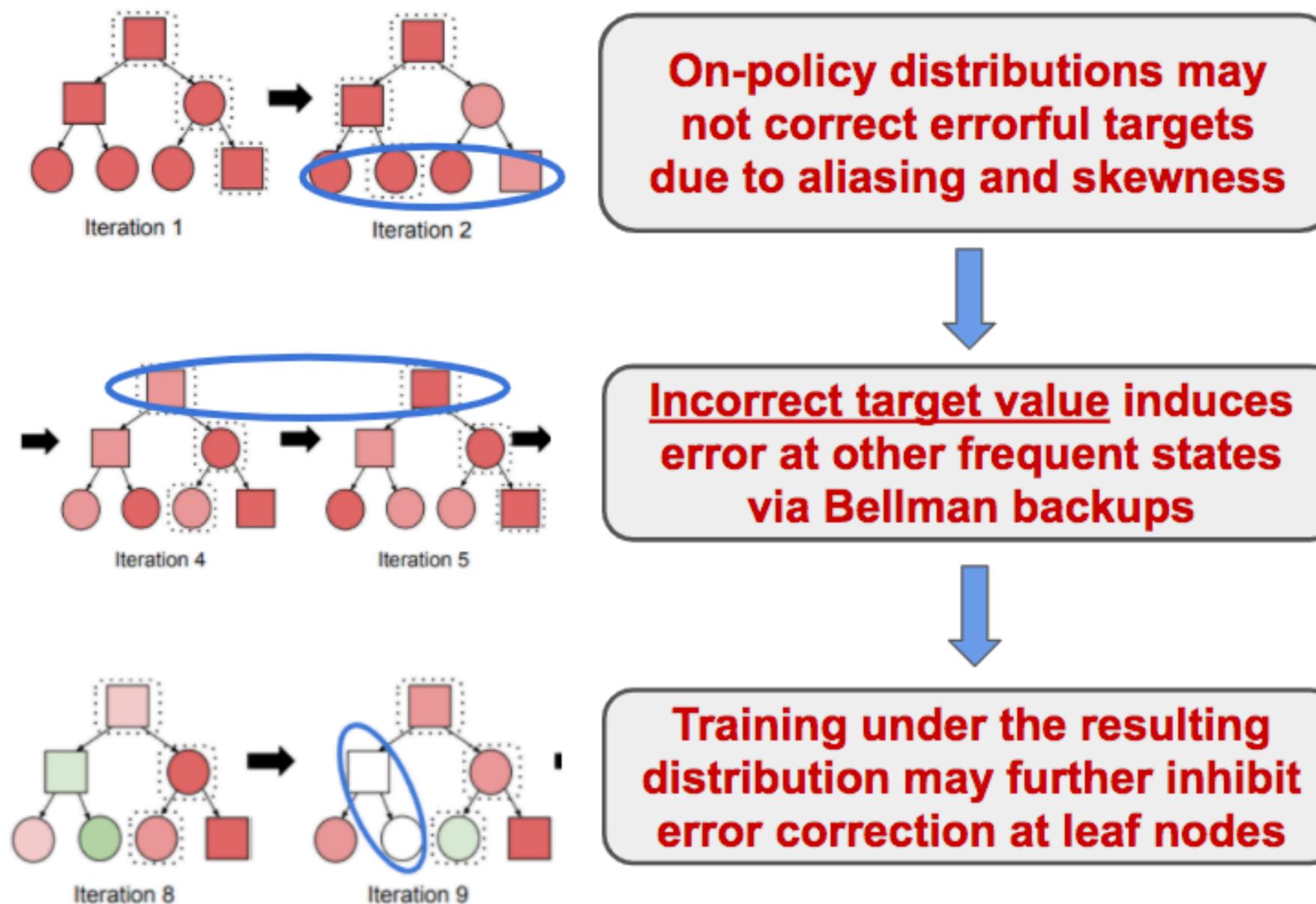
Q-Learning with On-Policy Data Collection

$$\mathcal{E}_k = |Q_k - Q^*|$$

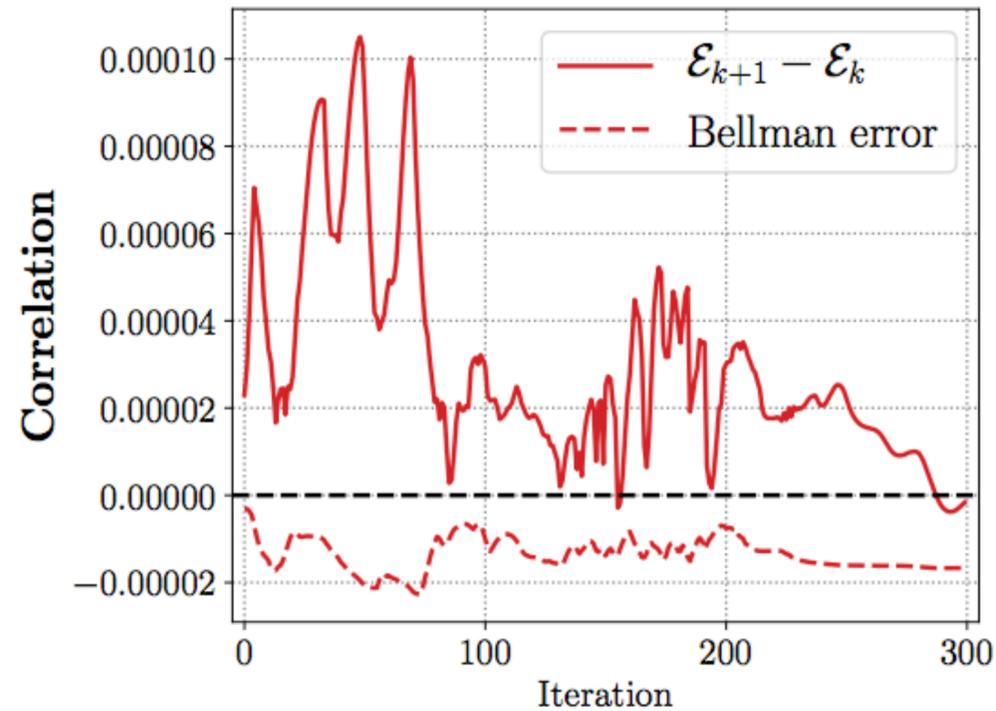


Function Approximation +
On-policy distribution =
Incorrect targets

Summary of the Tree MDP Example



Q-Learning with On-Policy Data Collection



$$d^{\pi_k}(s, a)$$

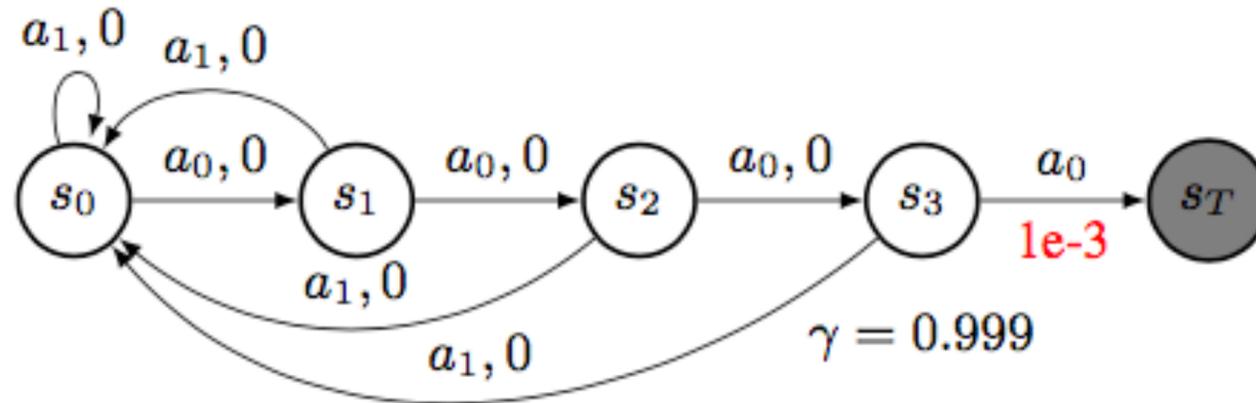
$$\mathcal{E}_k = |Q_k - Q^*|$$

Policy visitation corresponds to reduced Bellman error, but overall error may increase!

$$Q(s, a) = [w_1, w_2]^T \phi(s, a)$$

$$\phi(\cdot, a_0) = [1, 1]$$

$$\phi(\cdot, a_1) = [1, 1.001]$$



$$[w_1, w_2]_{\text{init}} = [0, 1e - 4]$$

Check that overall error increases!

What does this tell us?

- While on-policy data collection is sufficient for “error correction”/ convergence in the absence of function approximation, function approximation can make it ineffective in error correction...
- We saw that more gradient updates under such a distribution lead to poor features (due to the implicit under-parameterization phenomenon), which can potentially lead to poor solutions after that....
- We saw that entropic distributions are better — but we have no control over what comes in the buffer, unless we actually change the exploration strategy, so can we do better?

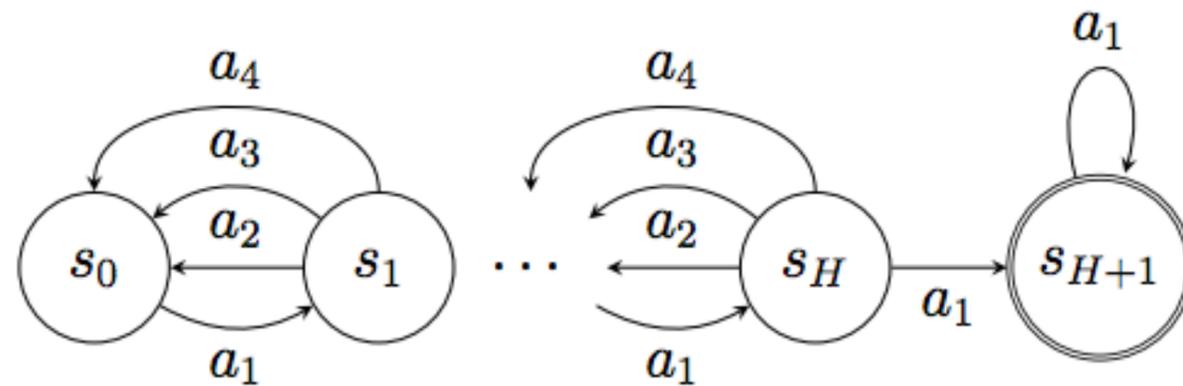
Part 2: Policy Gradient Algorithms

Initial State Distribution in Policy Gradients

Policy gradients maximize expected value at the initial state

$$\max_{\pi} J(\pi) = V^{\pi}(s_0)$$

$$\nabla_{\theta} V^{\pi_{\theta}}(s_0) = \frac{1}{1-\gamma} \mathbb{E}_{s \sim d_{s_0}^{\pi_{\theta}}} \mathbb{E}_{a \sim \pi_{\theta}(\cdot|s)} [\nabla_{\theta} \log \pi_{\theta}(a|s) Q^{\pi_{\theta}}(s, a)].$$



Policy gradient can be nearly 0, leading to poor solutions!

Ignore γ^t ? Reward shaping? re-weighting?

Proposition 4.1 (Vanishing gradients at suboptimal parameters). Consider the chain MDP of Figure 2, with $H + 2$ states, $\gamma = H/(H + 1)$, and with the direct policy parameterization (with $3|S|$ parameters).

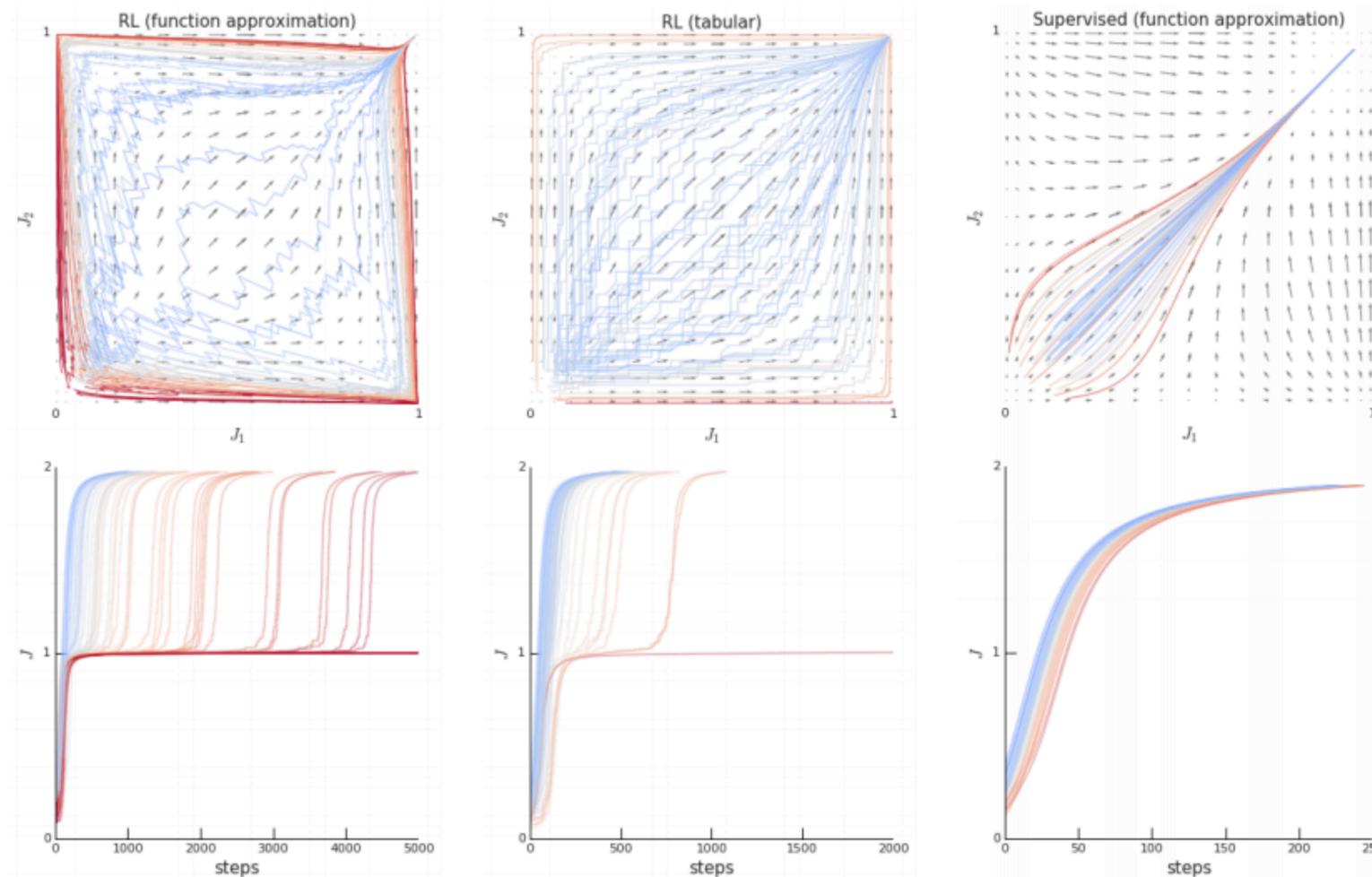
Poor solutions are sort of “equally poor” and the depth of the chain makes it hard to find any gradient of improvement

where $\nabla_{\theta}^k V^{\pi_{\theta}}(s_0)$ is a tensor of the k_{th} order derivatives of $V^{\pi_{\theta}}(s_0)$ and the norm is the operator norm of the tensor.⁴ Furthermore, $V^*(s_0) - V^{\pi_{\theta}}(s_0) \geq (H + 1)/8 - (H + 1)^2/3^H$.

Policy Gradient Plateaus: What and Why?

Policy gradient + function approximation + on-policy data

$$J_1 + J_2$$



Might end up optimizing one component of the objective more than others

If you hit a saddle point of the expected return function (corners), then stays there

Initialization, etc become important now!

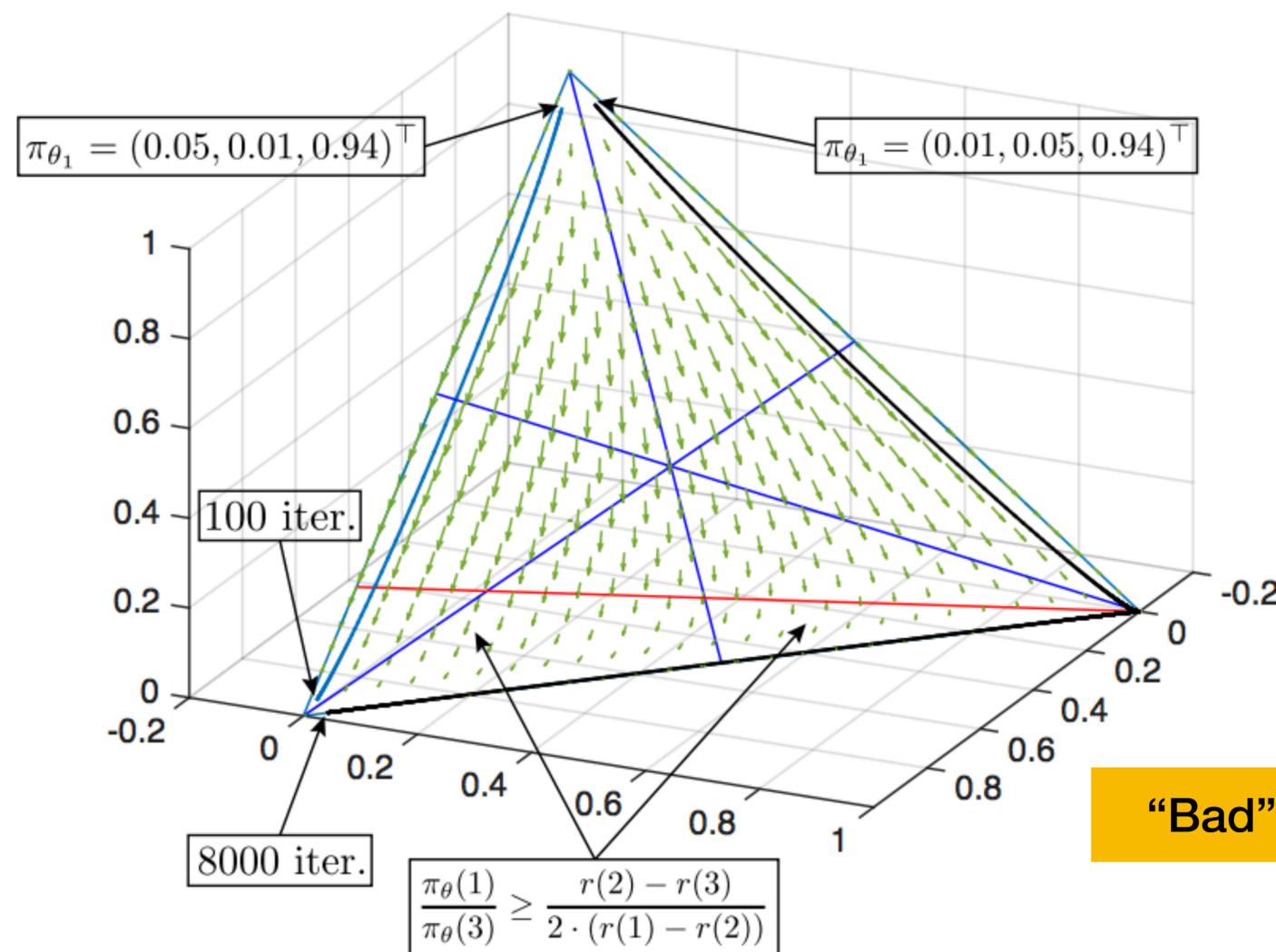
$$\pi_{\theta}(a|s) = \frac{\exp\{\theta(s, a)\}}{\sum_{a'} \exp\{\theta(s, a')\}}$$

Also affected by attraction to suboptimal solutions during training!

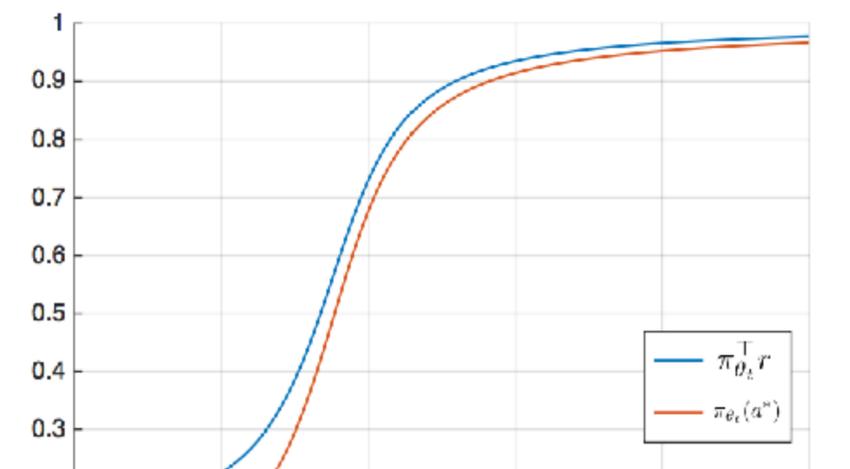
Importance of Initialization and Rewards

Reward values affect policy gradient methods a lot!

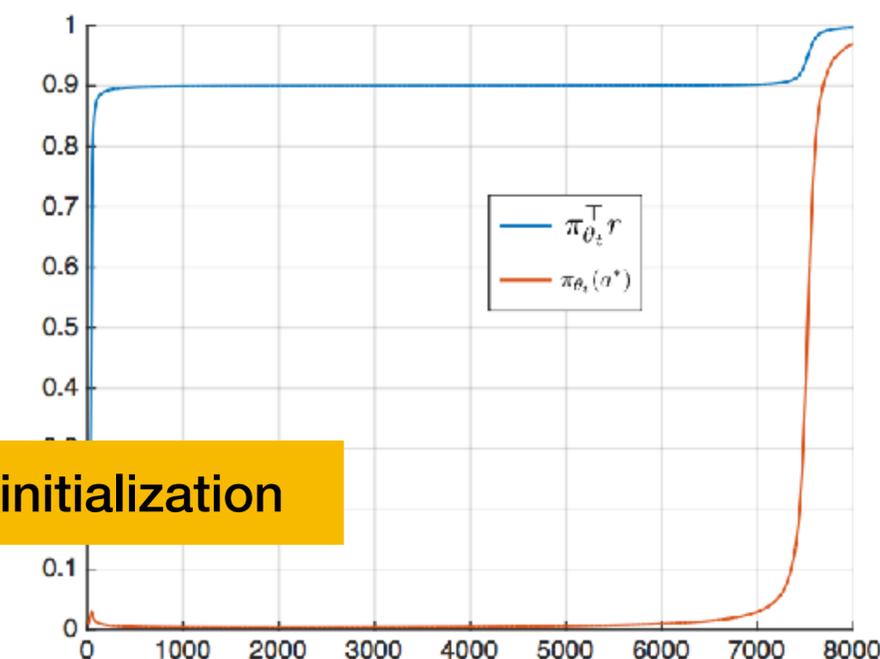
Consider a 3-armed bandit (1-step RL) problem with arm 1 being the optimal arm.



“Good” initialization



“Bad” initialization



Initialization matters, reward values matter. Also matter in offline settings.

Summary and Takeaways

- Overfitting in RL consists of more than just sampling error in standard supervised learning — we discussed how the update in Q-learning leads to poor solutions.
- Data-distributions matter a lot for RL problems: for both Q-learning algorithms and policy-gradient algorithms, only started understanding the surface in this domain
- Iterated training and changing objectives can be heavily affected by initialization, coverage, function approximation, etc in both Q-learning and policy gradient methods

Several open questions along these lines, have the potential to lead to stable and efficient algorithms